

FULL AVERAGING OF FUZZY IMPULSIVE DIFFERENTIAL INCLUSIONS

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Abstract. In this paper the substantiation of the method of full averaging for fuzzy impulsive differential inclusions is studied. We extend the similar results for impulsive differential inclusions with Hukuhara derivative [23], for fuzzy impulsive differential equations [18], and for fuzzy differential inclusions [26].

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